## Expected value

1) 

Hugo plans to buy packs of baseball cards until he gets the card of his favorite player, but he only has enough money to buy at most 4 packs. Suppose that each pack has probability 0.2 of containing the card Hugo is hoping for.

Let the random variable $X$ be the number of packs of cards Hugo buys. Here is the probability distribution for $\boldsymbol{X}$ :

| $X=$ \# of packs | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| $P(X)$ | 0.2 | 0.16 | 0.128 | $?$ |

Find the indicated probability.
$P(X \geq 2)=$ $\qquad$
2)

A certain lottery ticket costs $\$ 2$, and the back of the ticket says, "The overall odds of winning a prize with this ticket are $1: 50$, and the expected return for this ticket is $\$ 0.95$."

Which interpretations of the expected value are correct?

Choose all answers that apply:
(A) The probability that one of these tickets wins a prize is 0.95 , on average.
(B) Someone who buys this ticket is most likely to win $\$ 0.95$.
C. If we looked at many of these tickets, the average return would be about $\$ 0.95$ per ticket.
(D)

If 1,000 people each bought one of these tickets, they'd expect a net gain of about $\$ 950$ in total.
3)

A construction company is considering submitting bids for two contracts. It will cost the company $\$ 10,000$ to prepare and submit the bids, and if won, each bid would produce $\$ 50,000$ of income to the company. The company estimates that it has a $10 \%$ chance of winning any given bid.

Here is the probability distribution of $X=$ the number of bids the company wins, and $M=$ the amount of money the company profits from the bids.

| $X=$ the number of bids won | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- |
| $M=$ profit |  |  |  |
| Probability |  |  |  |

Calculate the mean of $M$.
4)

A "Pick 4" lottery game involves drawing 4 numbered balls from separate bins each containing balls labeled from 0 to 9 . So there are 10,000 possible selections in total: $0000,0001,0002, \ldots, 9998$, 9999.

Players can choose to play a "straight" bet, where the player wins if they match all 4 digits in the correct order. The lottery pays $\$ 4,500$ on a successful $\$ 1$ straight bet.

Let $X$ represent a player's net gain on a $\$ 1$ straight bet.

Calculate the expected net gain $E(X)$.
Hint: The expected net gain can be negative.

5)

An electronics store gives customers the option of purchasing a protection plan when customers buy a new television. The customer pays $\$ 80$ for the plan, and if their television is damaged or stops working, the store will replace it for no additional charge. The store knows that $2 \%$ of customers who buy this plan end up needing a replacement that costs the store $\$ 1,200$ each.

Here is a table that summarizes the possible outcomes from the store's perspective:

| Replacement? | Cost | Net gain $(X)$ |
| :--- | ---: | ---: |
| Yes | $\$ 1,200$ | $-\$ 1,120$ |
| No | $\$ 0$ | $\$ 80$ |

Let $X$ represent the store's net gain from one of these plans.
Calculate the expected net gain $E(X)$.

